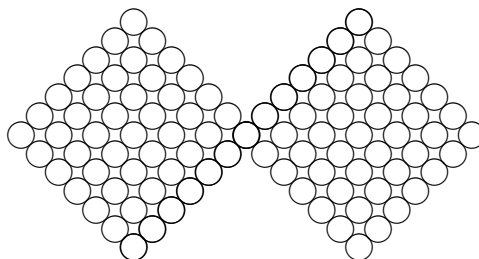


# 97 Ninety-Seven XCVII



Corresponding ordinal: ninety-seventh.

The number 97 is the forty-ninth odd number.

The number 97 is the twenty-fifth prime number. This is our final prime, but not the last prime in the universe. Euclid showed that there is always another prime. The number  $2^{43112609} - 1$ , a number that is 12,978,189 digits long, is currently the largest known prime. It was shown to be prime in 2008.

The number 97 has only two divisors: 1 and 97.

The number 97 is the seventy-fourth deficient number.

As a sum of four or fewer squares:  $97 = 4^2 + 9^2 = 5^2 + 6^2 + 6^2 = 1^2 + 4^2 + 4^2 + 8^2 = 2^2 + 2^2 + 5^2 + 8^2 = 3^2 + 4^2 + 6^2 + 6^2 = 4^2 + 4^2 + 4^2 + 7^2$ .

As a sum of nine or fewer cubes:  $97 = 6 \cdot 1^3 + 3^3 + 4^3 = 1^3 + 4 \cdot 2^3 + 4^3 = 2 \cdot 2^3 + 3 \cdot 3^3$ .

As the difference of two squares:  $97 = 49^2 - 48^2$ .

The number 97 appears in two Pythagorean triples:  $[65, 72, 97]$  and  $[97, 4704, 4705]$ . They are both primitive, of course.

As a sum of three odd primes:  $97 = 3 + 5 + 89 = 3 + 11 + 83 = 3 + 23 + 71 = 3 + 41 + 53 = 3 + 47 + 47 = 5 + 13 + 79 = 5 + 19 + 73 = 5 + 31 + 61 = 7 + 7 + 83 = 7 + 11 + 79 = 7 + 17 + 73 = 7 + 19 + 71 = 7 + 23 + 67 = 7 + 29 + 61 = 7 + 31 + 59 = 7 + 37 + 53 = 7 + 43 + 47 = 11 + 13 + 73 = 11 + 19 + 67 = 11 + 43 + 43 = 13 + 13 + 71 = 13 + 17 + 67 = 13 + 23 + 61 = 13 + 31 + 53 = 13 + 37 + 47 = 13 + 41 + 43 = 17 + 19 + 61 = 17 + 37 + 43 = 19 + 19 + 59 = 19 + 31 + 47 = 19 + 37 + 41 = 23 + 31 + 43 = 23 + 37 + 37 = 29 + 31 + 37$ .

The numbers 97, 907, 9007, 90007, and 900007 are primes.

## 2 Chapter 97 Ninety-Seven XCVII

There are 97 primes composed of exactly three distinct digits.

The number 97 is the largest prime that is less than the sum of the squares of its digits. (Prime Curios) In fact, 97, 98, and 99 are all less than the sum of the squares of their digits, while every number greater than 99 is greater than the sum of the squares of its digits.

There are exactly 97 ways to form two fractions that add up to 1 using the digits 0 through 9 exactly once. (Prime Curios) Two examples:  $1/2 + 3485/6970$  and  $24/63 + 507/819$ .

The number 97 is the smallest prime whose Roman numeral, XCVII, has prime alphabetical value:  $24 + 3 + 22 + 9 + 9 = 67$ . (Number Gossip) The next such prime is 107. Primes of this form that are interesting years are 1453, 1861, and 2011.

The “Wreck of the Old 97” is a famous ballad about a train wreck near Danville, Virginia in 1903. Sample lyrics: “He was found in the wreck with his hand on the throttle; Scalded to death by the steam.” and “Never speak harsh words to your true lovin’ husband; He may leave you and never return.”

In the only perfect game in World Series history, Don Larsen threw 97 pitches.